SEMICONDUCTOR RADIATION DETECTOR MATERIALS: FACTS VERSUS FICTION

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General References


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Compound semiconductor radiation detectors

Alan Owens*, A. Peacock

Abstract

We discuss the potential benefits of using compound semiconductors for the detection of X-and g ray radiation. While Si and Ge have become detection standards for energy dispersive spectroscopy in the laboratory, their use for an increasing range of applications is becoming marginalized by one or more of their physical limitations; namely the need for ancillary cooling systems or bulky cryogenics, their modest stopping powers and radiation intolerance. **Compound semiconductors encompass such a wide range of physical properties that it is technically feasible to engineer a material to any application.** Wide band-gap compounds offer the ability to operate in a wide range of thermal and radiation environments, whilst still maintaining sub-keV spectral resolution at hard X-ray wavelengths. Narrow band-gap materials, on the other hand, offer the potential of exceeding the spectral resolution of both Si and Ge, by as much as a factor of 3…
Topics to be discussed

• The Ionization Chamber
• Semiconductor Properties
• Interaction of Radiation with Semiconductors
• P-N-Junctions
• Detector Materials: Ge, Si, (GaAs)
• Room Temperature and High Z Materials: CdTe, CdZnTe, HgI₂, GaAs, AlSb
• Conclusions
The Ionization Chamber: Displacement Current and Charge Collection

Applies to:
- reverse biased p-n or p-i-n junction,
- resistive detectors,
- gas ionization chambers,
- proportional counters, etc.
The Ionization Chamber: Operating Principle

The field lines of a charge in volume V end on the electrodes and "influence" an electric charge. The relative quantities of charge influenced on each electrode depends only on the geometry. When the charge moves (in an externally applied field), the relative quantities of influenced charge change, forming a displacement current. When the charge stops moving, the displacement current stops flowing. Charge may stop flowing because it gets "trapped" at a defect center or gets "collected" at a contact. In a typical p-n junction, charge ideally flows to one of the electrodes. In a resistive detector, charge arriving at one electrode may lead to the injection of a new charge at the opposite electrode.

We define the "photoconductive" gain: \[ G = \frac{\ell}{L} \]

- \( \ell \) = average distance traveled by a free charge
- \( L \) = inter electrode distance

Note: For a high resolution detector, a fixed, constant gain is required (for p-n junctions: \( G = 1.00 \))
SEMICONDUCTOR PROPERTIES

Diamond Crystal Lattice: [100] Direction
Silicon

A) Real space structure,
[100] projection
(The sign = represents the two electrons in each bond.)

B) Electronic band structure
(CB = conduction band,
VB = valence band)
Donor doping (e.g., phosphorus on Si sites) provides extra electrons which can move into the conduction band or compensate an acceptor;

Acceptor doping (e.g., aluminum on Si sites) creates holes which can move into the valence band or compensate a donor.
Bandstructures of Ge and Si are *indirect*.

$k$ -vector
GaAs Bandstructure is direct
Temperature Effects

Radiation detector performance is affected by temperature in several ways. Two important ones are:

A. Generation of free electrons and holes by thermal ionization across the bandgap. This affects the bias current I (also called "leakage" or "dark" current) through the detector. This current is a source of electrical noise, in its simplest case "shot" noise ($I^2df = 2eIdf$; $e =$ charge of the electron, $f =$ frequency)

B. Trapping and de-trapping of the free charge carriers at defect or doping related energy levels in the bandgap.
A. Free Carrier Concentration

At finite temperatures a very small number of bonds in a crystal is broken. For each broken bond there exists a mobile electron and a mobile hole. The concentration of these electrons and holes is called *intrinsic carrier concentration* $n_i$:

$$n_i^2 = N_c N_v \exp \left(-\frac{E_{\text{gap}}}{k_B T}\right)$$

- $N_c$ = conduction band effective density of states
- $N_v$ = valence band effective density of states
- $k_B$ = Boltzmann's constant = $8.65 \times 10^{-5} \text{ eV/K}$
- $E_{\text{gap}}$ = energy gap (Si: 1.1 eV, Ge: 0.7 eV, GaAs = 1.42 eV, CdTe: 1.47 eV, Hgl₂: 2.13 eV, AlSb: 1.58 eV)

- $n_i$ (Si, 300K) = $2 \times 10^{10} \text{ cm}^{-3}$
- $n_i$ (Ge, 300K) = $3 \times 10^{13} \text{ cm}^{-3}$
- $n_i$ (GaAs, 300K) = $10^7 \text{ cm}^{-3}$
The thermal generation of electrons and holes gives rise to the reverse (also called "leakage" or "dark") current. This current constitutes a source of electronic noise.

**Consequences**

- Because of the small bandgap, Ge diodes must be cooled in order to achieve sufficiently low reverse currents.
- Si diodes have to be cooled only for high resolution applications.
- CdTe, CdZnTe, GaAs, AlSb and Hgl₂ do not require cooling.
Arrhenius plot of the intrinsic carrier concentration of some major semiconductors
# Semiconductor Band Gaps

<table>
<thead>
<tr>
<th>Band-gap energy (eV)</th>
<th>Elemental group IVB</th>
<th>Binary IV–IV compounds</th>
<th>Binary III–V compounds</th>
<th>Binary II–VI compounds</th>
<th>Binary IV–VI compounds</th>
<th>Binary n–VIIB compounds</th>
<th>Ternary compounds</th>
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<tbody>
<tr>
<td>0.00–0.25</td>
<td>Sn</td>
<td>InSb</td>
<td>HgTe</td>
<td>HgSe</td>
<td>PbSe, PbS, PbTe</td>
<td>HgCdTe</td>
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<td>0.50–0.75</td>
<td>Ge</td>
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<td>CdTe</td>
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<tr>
<td>1.50–1.75</td>
<td>BP, InN</td>
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<td>1.75–2.00</td>
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<td>AlAs</td>
<td>HgS</td>
<td>HgI₂</td>
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<td>GaP, AlP</td>
<td>ZnTe, CdS</td>
<td>PbI₂</td>
<td>TlBr</td>
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<td>ZnSe</td>
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<td>MnSe</td>
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<td>MgTe, MnS</td>
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<td>MgSe, ZnS</td>
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<td>4.75–5.00</td>
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<td>5.10–5.25</td>
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</tbody>
</table>

*Note: Compounds are listed in order of increasing band-gap energy.*
Electrons and holes are created in ionization events caused by radiation. In order to be detected they have to traverse the detector crystal all the way to their respective electrodes. On the way they encounter impurities, some of which are charged. Trapping and release from such ionized impurities is described as follows:

emission rate $e$ (per level) of a carrier to the nearest band:

$$e = \sigma <v> N_{\text{band}} \exp \left(-\frac{E}{k_B T}\right)$$

with

$\sigma$ = carrier capture cross-section (cm$^2$)

$<v>$ = average thermal velocity = $(3kT/m^*)^{1/2}$

$N_{\text{band}}$ = effective density of states

$= 2 \left(2\pi m^*kT/h^2\right)^{3/2}$

$k_B$ = 8.65 \times 10^{-5} \text{ eV/K}

$E$ = binding energy of a particular level
Shallow dopant levels in Si (E ~ 45 meV) or Ge (E ~ 10 meV) do not trap charge for any significant length of time at temperatures above 77 K (liquid nitrogen).

However, already very small concentrations of deep levels (E > 100 meV) trap charge effectively and do not release it within the collection time. The fluctuations in this charge loss lead to asymmetric peaks in the energy spectrum.
1: trapping of an electron on a deep level.

either 2: recombination of the trapped electron with a free hole.

or 3: detrapping after a time $t$. 

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The Origin of Deep Level Traps

- Deep level *impurities*: e.g., Au and Fe in Si, transition metals, Cu in Ge, etc.
- *Native defects*: vacancies, interstitials, antisites in compound semiconductors (As on Ga sites: $\text{As}_{\text{Ga}}$); the concentration of antisites is strongly affected by stoichiometry (e.g., SI GaAs has $10^{16} \text{ cm}^{-3} \text{ As}_{\text{Ga}}$).

Deep levels are localized in real space but extended in k-space. Their binding energies $E \gg 3/2kT$. The capture cross sections vary between $10^{-12}$ and $10^{-26} \text{ cm}^2$. 
Deep Level in k-Space
Electric Charge Transport

At low electric fields the carrier velocity \( \vec{v} \) is proportional to the electric field \( \vec{E} \):

\[
\vec{v} = \mu \vec{E}
\]

The mobility \( \mu \) rises with decreasing temperature:

<table>
<thead>
<tr>
<th></th>
<th>electrons</th>
<th>holes</th>
<th>temp (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \mu_{\text{Si}} ):</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(cm(^2)/Vs)</td>
<td>21,000</td>
<td>11,000</td>
<td>77</td>
</tr>
<tr>
<td></td>
<td>1,350</td>
<td>480</td>
<td>300</td>
</tr>
<tr>
<td>( \mu_{\text{Ge}} ):</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(cm(^2)/Vs)</td>
<td>40,000</td>
<td>40,000</td>
<td>77</td>
</tr>
<tr>
<td></td>
<td>3,900</td>
<td>1,900</td>
<td>300</td>
</tr>
</tbody>
</table>

At high electric fields **velocity saturation** occurs. The carriers emit phonons* at a rapidly increasing rate and the velocity becomes almost constant. It is interesting to note that the saturation velocity for most semiconductors lies around \( 10^7 \text{cm/s} \).

* Lattice vibrations (quantized \( E = h\omega \) )
Free Carrier Velocity as a Function of the Electric Field

Drift velocity as a function of electric field applied parallel to the ⟨111⟩ crystallographic direction. Absolute temperature is the parameter for the different curves. (a) Electrons in silicon; (b) holes in silicon; (c) electrons in germanium; (d) holes in germanium.

The $\mu\tau$ Product

- Mobility $\mu$: $v = \mu E$
- Carrier lifetime $\tau$: Average time a minority carrier lives
- Distance $d$ a carrier travels: $d = \mu \tau E$
- $d$ should be much larger than the intercontact distance
### Semiconductor Properties

Compilation of the physical properties of compound semiconductors for which spectroscopic results have been reported, grouped according to density.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Si</th>
<th>4H-SIC</th>
<th>InP</th>
<th>GaAs</th>
<th>Ge</th>
<th>Cd$<em>{0.15}$Mn$</em>{0.85}$Te</th>
<th>Cd$<em>{0.15}$Zn$</em>{0.85}$Te</th>
<th>Zn$<em>{0.15}$Cd$</em>{0.85}$Te</th>
<th>Zn$<em>{0.15}$Cd$</em>{0.85}$Se</th>
<th>CdTe</th>
<th>PbTe</th>
<th>HgTe</th>
<th>TlBr</th>
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</thead>
<tbody>
<tr>
<td>Density (g/cm$^3$)</td>
<td>2.33</td>
<td>3.21</td>
<td>4.78</td>
<td>5.32</td>
<td>5.33</td>
<td>5.8</td>
<td>5.58</td>
<td>5.81</td>
<td>5.85</td>
<td>6.2</td>
<td>6.4</td>
<td>7.56</td>
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<tr>
<td>Average atomic number(s)</td>
<td>14</td>
<td>10</td>
<td>32</td>
<td>31.5</td>
<td>32</td>
<td>49</td>
<td>49.1</td>
<td>41</td>
<td>50</td>
<td>63</td>
<td>62</td>
<td>58</td>
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<tr>
<td>Band gap (eV)</td>
<td>1.12</td>
<td>3.26</td>
<td>1.35</td>
<td>1.43</td>
<td>0.67</td>
<td>1.73</td>
<td>1.572</td>
<td>1.73</td>
<td>1.44</td>
<td>2.32</td>
<td>2.15</td>
<td>2.68</td>
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<td>Pair creation energy (eV)</td>
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<td>7.8</td>
<td>4.2</td>
<td>4.2</td>
<td>2.96</td>
<td>2.12</td>
<td>4.64</td>
<td>5.5</td>
<td>4.43</td>
<td>4.9</td>
<td>4.2</td>
<td>6.5</td>
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<tr>
<td>Electron mobility (cm$^2$V$^{-1}$s$^{-1}$)</td>
<td>14000</td>
<td>10000</td>
<td>4600</td>
<td>8000</td>
<td>3900</td>
<td>10090</td>
<td>840</td>
<td>1100</td>
<td>8</td>
<td>100</td>
<td>30</td>
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<tr>
<td>Hole mobility (cm$^2$V$^{-1}$s$^{-1}$)</td>
<td>19000</td>
<td>115</td>
<td>150</td>
<td>400</td>
<td>1900</td>
<td>120</td>
<td>75</td>
<td>100</td>
<td>2</td>
<td>4</td>
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<tr>
<td>Electron lifetime (s)</td>
<td>&gt; 10$^{-3}$</td>
<td>5 × 10$^{-7}$</td>
<td>1.5 × 10$^{-8}$</td>
<td>10$^{-3}$</td>
<td>&gt; 10$^{-3}$</td>
<td>3 × 10$^{-6}$</td>
<td>10$^{-7}$</td>
<td>3 × 10$^{-6}$</td>
<td>10$^{-7}$</td>
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<td>2 × 10$^{-10}$</td>
<td>10$^{-7}$</td>
<td>10$^{-6}$</td>
<td>10$^{-9}$</td>
<td>2 × 10$^{-6}$</td>
<td>3 × 10$^{-7}$</td>
<td>1 × 10$^{-5}$</td>
<td>3.7 × 10$^{-5}$</td>
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<tr>
<td><strong>Electron μτ product (cm$^2$V$^{-1}$)</strong></td>
<td>&gt; 1</td>
<td>4 × 10$^{-4}$</td>
<td>5 × 10$^{-6}$</td>
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<td>1 × 10$^{-5}$</td>
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<td><strong>Hole μτ product (cm$^2$V$^{-1}$)</strong></td>
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<td>8 × 10$^{-5}$</td>
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<td>&gt; 1</td>
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<td>3 × 10$^{-7}$</td>
<td>4 × 10$^{-3}$</td>
<td>2 × 10$^{-5}$</td>
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</table>

**Crystal structure**
- Cubic
- Hexagonal
- Cubic (ZB)
- Cubic (ZB) (Cubic)
- Hexagonal
- Cubic (ZB) (Wurtzite)
- Cubic (ZB) (Hexagonal, Tetragonal)
- Cubic (CsCl)

<table>
<thead>
<tr>
<th>Lattice constant (Å)</th>
<th>Cubic</th>
<th>Hexagonal</th>
<th>Cubic (ZB)</th>
<th>Cubic (ZB) (Cubic)</th>
<th>Hexagonal</th>
<th>Cubic (ZB) (Wurtzite)</th>
<th>Cubic (ZB) (Hexagonal, Tetragonal)</th>
<th>Cubic (CsCl)</th>
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<td></td>
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<td>5.633</td>
<td>5.64613</td>
<td>4.2999 (u)</td>
<td>7.0109 (c)</td>
<td>4.37 (u)</td>
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<td>2546</td>
<td>460</td>
<td>750</td>
<td>692</td>
<td>?</td>
<td>90-130</td>
<td>60</td>
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<td>1238</td>
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<td>9.7</td>
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<td>12.8</td>
<td>16</td>
<td>10</td>
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<td>8.8</td>
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<td>&lt; 10$^4$</td>
<td>&gt; 10$^4$</td>
<td>10$^5$</td>
<td>10$^7$</td>
<td>50</td>
<td>10$^{15}$</td>
<td>3 × 10$^{10}$</td>
<td>10$^5$</td>
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<td>1/e absorpt. Depth (μm) at 10 keV</td>
<td>0.127</td>
<td>0.128</td>
<td>0.020</td>
<td>0.051</td>
<td>0.050</td>
<td>0.019</td>
<td>0.011</td>
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<td>at 1000 keV</td>
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<td>17.90</td>
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<td>3.51</td>
<td>1.5</td>
<td>1.01</td>
<td>1.5</td>
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<td>Typ. FWHM ΔE (keV) at 60 keV</td>
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<td>2.7</td>
<td>12</td>
<td>0.7</td>
<td>0.3</td>
<td>21</td>
<td>1.8</td>
<td>1.5</td>
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<td>Intrinsic FWHM ΔE (keV) at 60 keV (Fano noise)</td>
<td>0.415</td>
<td>0.642</td>
<td>0.443</td>
<td>0.439</td>
<td>0.250</td>
<td>0.530</td>
<td>0.530</td>
<td>0.393</td>
</tr>
<tr>
<td>Typical thickness (μm)</td>
<td>0.3</td>
<td>0.3</td>
<td>0.2</td>
<td>0.2</td>
<td>0.2</td>
<td>0.5</td>
<td>0.1</td>
<td>2</td>
</tr>
</tbody>
</table>

**Note:** For comparison, the properties of the elemental semiconductors, Si and Ge are also listed. The Fano noise was calculated using the "best" reported values of the Fano factor, otherwise a value of 0.14 was assumed.

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2/15/2006

E. E. Haller 26
Interaction of Radiation with Semiconductors

photons:  - photo effect
         - Compton effect
         - pair production (E > 2m_e c^2)

particles: - ionization  →  e/h pairs

energetic electrons  →  e/h pairs
Photon Absorption in Ge

\[ I_x = I_o \exp(-\alpha x) \]

\( \alpha \) = linear absorption coefficient

Absorber
Si, Ge, etc.
Photon Absorption in Si
Requirements for the Ideal Solid State Ionization Chamber

- excellent charge transport (no trapping, complete collection)
- no free mobile charges in the absence of radiation (i.e., low leakage current)
- linearity between the energy of the incident radiation and the number of e/h pairs
- maximum number of e/h pairs per unit energy
- high detection efficiency (large Z, large volume)
- short charge collection time (fast timing)
- convenient operating temperature
- position information (for some applications)
- inexpensive
P-N and P-I-N Junctions
The Asymmetric Planar N⁺-P-Junction (parallel plate capacitor)
The ionized shallow impurity levels constitute a space charge $e |N_A - N_D|$. Poisson's equation relates the potential $\phi$ to the charge:

$$\nabla^2 \phi = -e |N_A - N_D| / \varepsilon \varepsilon_o$$

$\varepsilon = $ dielectric constant, $\varepsilon_o = $ permittivity of vacuum

In one dimension:

$$\partial^2 \phi / \partial x^2 = -e |N_A - N_D| / \varepsilon \varepsilon_o$$

integrating twice leads to:

$$\phi = d^2 |N_A - N_D| \frac{e}{2 \varepsilon \varepsilon_o} = d^2 |N_A - N_D| C$$

$C_{Si} = 7.72 \times 10^{-8} \text{ Vcm}$

$C_{Ge} = 5.64 \times 10^{-8} \text{ Vcm}$

with:

$d = $ width of the depletion layer
Planar N⁺-P-Junction

For Ge junctions we find:

\[ V = d^2 \left| N_A - N_D \right| \times 5.64 \times 10^{-8} \text{ (Vcm)} \]

and for Si:

\[ V = d^2 \left| N_A - N_D \right| \times 7.72 \times 10^{-8} \text{ (Vcm)} \]

with

\( V \) = applied voltage (V)
\( d \) = depletion depth (cm)
\( \left| N_A - N_D \right| \) = net-impurity concentration (cm⁻³)

**EXAMPLE**: Planar P-I-N Detector

\( d = 2 \text{ cm}, V = 3000 \text{V} \)

What has \( \left| N_A - N_D \right| \) to be for full depletion?

Ge: \( 1.33 \times 10^{10} \text{ cm}^{-3} \)

Si: \( 9.7 \times 10^9 \text{ cm}^{-3} \)

These are extremely small concentrations compared to \( \sim 4 \times 10^{22} \text{ Ge or Si per cm}^3 \)!
Ultra-Pure Semiconductors

Motivation:
• Large depletion layers
• Low defect concentrations -> large lifetimes

Approach:
• Ultra-pure Ge grown from a synthetic silica crucible in 1 atm. of pure H$_2$
• Floating-Zone (FZ) Si grown in vacuum
• Liquid Phase Epitaxial GaAs
Sketch of a Modern CZ-puller

Jan Czochralski
Czochralski (CZ) Silicon single crystal;

8 inches (20 cm) in diameter and over 6 feet (~2 m) long;

Weight ~ 320 lb (145 kg)
Modern Silicon single crystal grown by the Czochralski technique at the Wacker Silitronix Hikari plant in Japan. The diameter is 12 inches (300 mm) and the length is over 4 feet.
An ultra-pure Germanium single crystal is being “pulled” from a melt contained in a silica crucible at 936°C. The atmosphere is pure Hydrogen. Heat is supplied by the water cooled radiofrequency (RF) coil surrounding the silica envelope. This bulk crystal growth technique carries the name of its inventor, “Jan Czochralski.”
Electrical conductivity is an accurate measure of the net-impurity concentration. The intrinsic conduction can be "turned-off" through cooling to liquid nitrogen temperature (77K).

\[ \rho = \frac{V}{I} \frac{A}{l} = \frac{1}{|N_A - N_D|} \frac{1}{\epsilon \mu} \]

- \(\rho\): electrical resistivity
- \(V\): voltage drop across segment of length \(l\)
- \(I\): injected current
- \(\epsilon\): charge of electron (1.6 x 10^{-19} As)
- \(\mu\): mobility (equal for \(e\) & \(h\) at 77K)
- \(A\): cross sectional area

\[ |N_A - N_D| = \frac{\epsilon \mu V}{A} \frac{l}{1} \]
Typical impurity profile of an ultra-pure Ge crystal. The acceptor aluminum (Al, dashed line) does not segregate in silica grown Ge, leading to a constant concentration. The donor phosphorus segregates (P, dotted line). In our particular example, the phosphorus concentration equals the aluminum concentration at 80% of the melt frozen and exceeds it beyond. In the Al dominated part, the crystal is p-type, in the P dominated type, the crystal is n-type.
GaAs Phase Diagram
The Floating Zone (FZ) crystal growth process is used for ultra pure silicon up to 6” in diameter. No crucible is used. The ambient is typically nitrogen but vacuum and argon have been used.
Silicon Floating Zone (FZ) crystal with 10 cm diameter is being pulled. The single turn RF heating coil creates the liquid “floating zone” between the lower part (single crystal) and the upper polycrystalline section.
Major Dimensions of Zoner VZA9

2/15/2006
Liquid Phase Epitaxy LPE
Multilayer LPE
Chemical Vapor Deposition or Vapor Phase Epitaxy
Metalorganic Chem. Vapor Deposition MOCVD
Molecular Beam Epitaxy (MBE)
High Bandgap-High Z Materials

• **Advantages:**
  – no limitations imposed by cooling requirements (medical probes, etc.)
  – small, efficient detection volume (medical probes, etc.)

• **Challenges:**
  – crystal growth is difficult: low purity and poor structural perfection
  – not all compound semiconductors can be doped p- and n-type
  – trapping and polarization
  – poor hole transport and short carrier lifetimes
  – limited crystal size
  – contact formation problems
  – chemical stability
## Properties of Compound Semiconductors

<table>
<thead>
<tr>
<th>Material</th>
<th>Atomic Number</th>
<th>Density g/cm³</th>
<th>Band gap (eV)</th>
<th>Knoop Hardness</th>
<th>Egap (eV)</th>
<th>Mobility, Ω-cm</th>
<th>μt (e) cm²/V</th>
<th>μt (h) cm²/V</th>
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<tbody>
<tr>
<td>Si</td>
<td>14</td>
<td>2.33</td>
<td>1.12</td>
<td>1150</td>
<td>3.62</td>
<td>&gt;10⁴</td>
<td>2.7x10⁻⁵</td>
<td>9.6x10⁻⁴</td>
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<td>CdTe</td>
<td>48, 52</td>
<td>6.2</td>
<td>1.44</td>
<td>45</td>
<td>4.35</td>
<td>10⁹</td>
<td>3.5x10⁻⁢⁴</td>
<td>2.3x10⁻⁴</td>
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<tr>
<td>CdZnTe</td>
<td>48, 30, 52</td>
<td>≈ 6</td>
<td>1.5 - 2.2</td>
<td>5.0 *</td>
<td>10¹¹</td>
<td>1x10⁻³</td>
<td>6x10⁻⁶</td>
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<tr>
<td>CdSe</td>
<td>18, 34</td>
<td>5.81</td>
<td>1.73</td>
<td>5.5 **</td>
<td>10⁸</td>
<td>7.2x10⁻⁶</td>
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<tr>
<td>CdZnSe</td>
<td>48, 30, 34</td>
<td>≈ 5.5</td>
<td>1.7-2.7</td>
<td>3x10⁴</td>
<td>1x10⁻⁴</td>
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<tr>
<td>HgI₂</td>
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<td>6.4</td>
<td>2.13</td>
<td>&lt;10</td>
<td>4.2</td>
<td>10³</td>
<td>8x10⁻⁵</td>
<td>4x10⁻⁶</td>
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<tr>
<td>TiBr</td>
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<td>2.2-2.8</td>
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<td>10¹⁰</td>
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<td>GaAs</td>
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<td>8x10⁻⁳</td>
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<td>27</td>
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<td>diamond</td>
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<td>TiBr</td>
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<td>1.6x10⁻⁵</td>
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<tr>
<td>Pbl₂</td>
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<td>6.2</td>
<td>2.32</td>
<td>&lt;10</td>
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<td>10¹¹</td>
<td>8x10⁻⁶</td>
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<td>InP</td>
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<td>1.35</td>
<td>535</td>
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<td>10⁷</td>
<td>4.8x10⁻⁴</td>
<td>&lt;1.5x10⁻⁵</td>
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<tr>
<td>ZnTe</td>
<td>30, 52</td>
<td>5.72</td>
<td>2.26</td>
<td>7.0 **</td>
<td>10¹⁰</td>
<td>1.4x10⁻⁵</td>
<td>7x10⁻⁵</td>
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<tr>
<td>HgBrI</td>
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<td>2.4-3.4</td>
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<td>5x10¹³</td>
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<td>a-Si</td>
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<tr>
<td>a-Se</td>
<td>34</td>
<td>4.3</td>
<td>2.3</td>
<td>7</td>
<td>10¹²</td>
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<td>1.4x10⁸</td>
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<td>BP</td>
<td>5, 15</td>
<td>2.9</td>
<td>2.1</td>
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<td>AlSb</td>
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<td>2.58</td>
<td>8.0**</td>
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<td></td>
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</tr>
</tbody>
</table>

(Note: materials are listed in order of decreasing μt (e) at room temperature.)

* estimated for 20% zinc
** estimated

Room Temperature and High Z Materials: CdTe, CdZnTe, Hgl$_2$ and GaAs

Major drivers for new detector materials development:

- room temperature operation ($E_{\text{gap}} > 1.4 \text{ eV}$)

- high efficiency (large Z)
The “Frisch Grid”: An Old Idea with Great Relevance and Promise

- Gas ionization chambers suffer from the same problem as many semiconductor detectors: $\mu \tau$ of one charge species (ions) is significantly lower than of the other charge species (electrons).

- **Solution:** the "Frisch Grid" (FG)

![Diagram of the Frisch Grid](image)
Reincarnation of the Frisch Grid as two sets of interdigitated contacts A and B

(a) C

(b) Induced Charge

Q

q_A

q_B

q_A - q_B

0

Distance

Courtesy P.N. Luke, LBNL
Operational Circuit for a Coplanar-Grid Detector

Courtesy P.N. Luke, LBNL
Recent Record

137Cs spectrum LBNL 7/23/05

Coplanar-grid CdZnTe detector
Volume: 1 cm³
Detector bias: -3000 V
Grid bias: 150 V
Shaping time: 2 µs
Temperature: -20°C

662 keV gamma:
FWHM: 6.20 keV (0.94%)
Peak/Compton: 14.4
Peak/valley: 150

Pulser:
FWHM: 4.04 keV

Courtesy P. N. Luke, LBNL
Conclusions

- The ideal semiconductor materials for all radiation detection applications does not exist but they can be approached closely.

- Certain material property requirements and application requirements are incompatible (e.g. bandgap: \textbf{large} for low leakage current but \textbf{small} for small energy per e/h pair).

- Si & Ge are the high resolution spectrometer materials. Detectors exhibit excellent stability, good efficiency, timing, etc.

- Thin epitaxial films (100-150 \textmu{}m) of high-purity GaAs ($|N_A-N_D| < 10^{12} \text{ cm}^{-3}$) have been grown by the LPE technique and early spectrometer results look promising. In contrast, semi-insulating (SI) GaAs deliberately contains very large concentrations of deep traps which make the material highly resistive and lead to extreme charge trapping.
Conclusions, cont.

- CdTe, CdZnTe & HgI$_2$ are room temperature materials. Low energy X rays can be detected with good resolution. Medium and high energy photons ($\gamma$-rays) still pose problems (after over 40 years of R&D!). Trapping and poor hole transport seem to be fundamental and/or related to material inhomogeneities and defects.


- The search for new semiconductor detector materials should remain realistic, balancing advantages and disadvantages (i.e., picking a good bandgap and a high Z is only part of the story!). The $\mu \tau$ product for electrons and for holes dominates charge collection.
3. Limitations of compound semiconductors

Unfortunately, compound semiconductors also suffer from several limitations, which do not affect their elemental counterparts. Perhaps the most severe of which is that one or both charge carriers suffer from poor transport—either through poor mobility or carrier lifetime. In this regard, the most useful figure of merit when comparing compounds is the mobility–lifetime product (\(\mu\tau\)). For the elemental semiconductors this is of the order of unity for both electrons and holes, whereas for compound semiconductors it rarely reaches greater than a few times \(10^{-4}\) for electrons and \(10^{-5}\) for holes—and these figures get worse with increasing Z. The cause can usually be traced to trapping centers caused by impurities, lack of stoichiometry, or for the softer materials, plastic deformation caused by mechanical damage during fabrication.
Thanks for your attention